## Exercise 1

- Example: suppose you start with 1 M of A and no $B$ and $C$. Which of the following series will lead to the greatest $[C]_{e q}$ ?
- $\quad\left(\right.$ Remember $\left.\mathrm{Keq}_{\mathrm{T}}=\mathrm{Keq}_{1} \times \mathrm{Keq}_{2}\right)$
- Series 1

$$
\begin{aligned}
\mathrm{A} & \rightleftharpoons \mathrm{~B} \Delta G^{\circ}=+18,85 \mathrm{~kJ} \mathrm{~mol}^{-1} ;
\end{aligned} K_{e q}=5 \times 10^{-4}, ~=-18,85 \mathrm{~kJ} \mathrm{~mol}^{-1} ; \quad K_{e q}=2 \times 10^{3}
$$

- Series 2

$$
\begin{aligned}
\mathrm{A} & \rightleftharpoons \mathrm{~B} \Delta G^{\circ}=-18,85 \mathrm{~kJ} \mathrm{~mol}^{-1} ; \quad K_{e q}=2 \times 10^{3} \\
\mathrm{~B} & \rightleftharpoons \mathrm{C} \Delta G^{\circ}=+18,85 \mathrm{~kJ} \mathrm{~mol}^{-1} ; K_{e q}=5 \times 10^{-4}
\end{aligned}
$$

Series 1:
At equilibrium:

$$
[A]+[B]+[C]=1 M
$$

$$
[\mathrm{B}] \mathrm{eq}=5 \times 10^{-4} \cdot[\mathrm{~A}] \mathrm{eq}
$$

$$
[\mathrm{C}] \mathrm{eq}=[\mathrm{A}] \mathrm{eq}
$$

$$
[\mathrm{A}] \mathrm{eq}+[\mathrm{A}] \mathrm{eq}+5 \times 10^{-4} \cdot[\mathrm{~A}] \mathrm{eq}=1 \mathrm{M}
$$

$$
=>[\mathrm{A}] \mathrm{eq}=0.5 \mathrm{M} ; \quad[\mathrm{B}] \mathrm{eq}=0.00025 \mathrm{M} ; \quad[\mathrm{C}] \mathrm{eq}=0.5 \mathrm{M}
$$

Series 2:
At equilibrium:

$$
\begin{aligned}
& {[\mathrm{B}] \mathrm{eq}=2 \times 10^{3} \cdot[\mathrm{~A}] \mathrm{eq}} \\
& {[\mathrm{C}] \mathrm{eq}=[\mathrm{A}] \mathrm{eq}} \\
& {[\mathrm{~A}] \mathrm{eq}+[\mathrm{A}] \mathrm{eq}+2 \times 10^{3} \cdot[\mathrm{~A}] \mathrm{eq}=1 \mathrm{M}} \\
& =>[\mathrm{A}] \mathrm{eq}=0.0005 \mathrm{M} ; \quad[\mathrm{B}] \mathrm{eq}=0.999 \mathrm{M} ; \quad[\mathrm{C}] \mathrm{eq}=0.0005 \mathrm{M}
\end{aligned}
$$

## Exercise 2: Experimental data

| $t$ | a | b |
| :--- | :--- | :--- |
| $(\mathrm{s})$ | $(\mathrm{mM})$ | $(\mathrm{mM})$ |
| 0 | 10. | 0. |
| 1 | 7.5274 | 2.4726 |
| 2 | 5.86997 | 4.13003 |
| 3 | 4.75896 | 5.24104 |
| 4 | 4.01422 | 5.98578 |
| 5 | 3.51501 | 6.48499 |
| 6 | 3.18038 | 6.81962 |
| 7 | 2.95607 | 7.04393 |
| 8 | 2.80572 | 7.19428 |
| 9 | 2.70493 | 7.29507 |
| 10 | 2.63737 | 7.36263 |
| 11 | 2.59208 | 7.40792 |
| 12 | 2.56172 | 7.43828 |
| 13 | 2.54137 | 7.45863 |
| 14 | 2.52773 | 7.47227 |
| 15 | 2.51859 | 7.48141 |
| 16 | 2.51246 | 7.48754 |
| 17 | 2.50835 | 7.49165 |
| 18 | 2.5056 | 7.4944 |
| 19 | 2.50375 | 7.49625 |
| 20 | 2.50252 | 7.49748 |

For a non catalyzed, chemical reaction; A<->B the following experimental data were obtained:

## Calculate:

- reaction rate at $t=5 \mathrm{~s}$
- Keq
- k(forward)
- k(reverse)
- mass action ratio at $t=5 \mathrm{~s}$
- reaction rate at $t=20 \mathrm{~s}$
- forward rate at $\mathrm{t}=20 \mathrm{~s}$
- reverse rate at $\mathrm{t}=20 \mathrm{~s}$


## Exercise 2: Solution


v $\quad-\mathrm{d}[\mathrm{A}] / \mathrm{dt}=$ slope of tangent at $\mathrm{t}=5$
$=0.4 \mathrm{mM} / \mathrm{s}$
$\boldsymbol{K}_{\text {eq }} \quad$ Equilibrium ratio of $[\mathrm{B}] /[\mathrm{A}]=$ 7.5/2.5 = 3
$v=k_{f}{ }^{*} a-k_{r}{ }^{*} b ;$
rate of reaction $(\mathrm{d}[\mathrm{A}] / \mathrm{dt})$ at $\mathrm{t}=0$;
$=-\mathrm{d}[\mathrm{A}] / \mathrm{dt}$
= slope of tangent at $\mathrm{t}=0$
$=3.0 \mathrm{mM} / \mathrm{s}$;
$k_{f}=3.0 / 10=0.31 / \mathrm{s}$
$\mathbf{k}_{\mathrm{r}} \quad \mathrm{K}_{\text {eq }}=\mathrm{k}_{\mathrm{f}} / \mathrm{k}_{\mathrm{r}}$;
$k_{r}=0.3 / 3=0.11 / \mathrm{s}$
$\Gamma \quad[B] /[A]$ at $t=5,6.48 / 3.52=1.84$
$\mathbf{V}_{20}$ at $\mathrm{t}=20$ the reaction is very close to equilibrium as is evident from the constant concentrations of $A$ and $B$, the velocity is close to 0

$$
\begin{array}{ll}
\mathbf{v}_{\mathrm{f}, \mathrm{t}=20} & \text { at } \mathrm{t}=20 \mathrm{v}_{\mathrm{f}}=0.3^{*} 2.5=0.75 \mathrm{mM} / \mathrm{s} \\
\mathbf{v}_{\mathrm{r}, \mathrm{t}=20} & \text { at } \mathrm{t}=20 \mathrm{v}_{\mathrm{r}}=0.1^{*} 7.5=0.75 \mathrm{mM} / \mathrm{s}
\end{array}
$$

## Exercise 3

- Calculate the maximal glucose gradient possible for a proton symport system with a stoichiometry of 2 protons per glucose molecule, if there is a pH difference of -0.3 (inside 6.7, outside 7.0), and the membrane potential is -200mV (negative inside).
- $R=8.31447 \mathrm{~J} / \mathrm{K} / \mathrm{mol}, T=298.17 \mathrm{~K}$, $F=96.485 \mathrm{~kJ} / \mathrm{V}$


## Exercise 3: Solution

- Calculate the maximal glucose gradient possible for a proton symport system with a stoichiometry of 2 protons per glucose molecule, if there is a pH difference of -0.3 (inside 6.7, outside 7.0), and the membrane potential is -200 mV (negative inside)

$$
\begin{array}{rlll}
p H= & { }^{10} \log \left[H^{+}\right] & \Delta G_{H^{+}} & =R T \ln \frac{\left[H^{+}\right]_{\text {in }}}{\left[H^{+}\right]_{\text {out }}}+Z F \cdot \Delta \psi \\
p H=7-> & {\left[H^{+}\right]=10^{-7}} & \Delta G_{H^{+}} & =8.31447 \cdot 298.17 \cdot \ln (1.995)+96.485 \cdot 10^{3} \cdot-0.2 \\
p H=6.7-> & {\left[H^{+}\right]=10^{-6.7}=1.995 \cdot 10^{-7}} & \Delta G_{H^{+}} & =1712.19-19297 \\
\Delta G_{H^{+}} & =-17584.8 \mathrm{~J} / \mathrm{mol} \mathrm{H}^{+} \\
\Delta G_{G l c} & =R T \ln \frac{[G l c]_{\text {in }}}{[G l c]_{\text {out }}} & \\
2 \cdot 17584.8 & =8.31447 \cdot 298.17 \cdot \ln \frac{[G l c]_{\text {in }}}{[G l c]_{\text {out }}} & \\
\frac{[G l c]_{\text {in }}}{[G l c]_{\text {out }}} & =1.45 \cdot 10^{6} &
\end{array}
$$

